



3. What is the limit as  $x \rightarrow \infty$  of the larger of the two roots of the equation  $x^2 - 2x + a = 0$  where  $a$  are real numbers and  $a > 0$  ?

- a)  $\frac{1}{2}$
- b)  $\frac{1}{\sqrt{a}}$
- c)  $\frac{1}{2\sqrt{a}}$
- d)  $\frac{1}{2a}$
- e) None of the above

4. Find the improper integral:  $\int_0^{\infty} \frac{1}{x^2 + 1} dx$

- a)  $\frac{\pi}{2}$
- b)  $\frac{\pi}{4}$
- c)  $\frac{\pi}{8}$
- d)  $\frac{\pi}{16}$
- e) None of the above

5. Let  $f(x) = \frac{1}{x^2 + 1}$ . Find  $\int_{-1}^1 f(x) dx$

- a)  $\frac{\pi}{4}$
- b)  $\frac{\pi}{2}$
- c)  $\frac{\pi}{8}$
- d)  $\frac{\pi}{16}$
- e) None of the above

6. Find the minimum value of the function

\_\_\_\_\_

- a)
- b)
- c)
- d)
- e) None of the above

7. Two half lines begin at the point  $(0, 0)$ , creating an angle of  $60^\circ$ . From the point  $(0, 0)$ , two particles start moving at the same time, each on a different half line. The first one is moving with the constant speed of  $1$  sec. The second is moving in such a way that its distance from the point can be expressed by  $\sqrt{t}$  where  $t$  is measured in meters and  $t$  in seconds. How fast is the distance between the two particles changing when the first particle is  $1$  meters from the point

- a)  $\frac{1}{2}$  sec
- b)
- c)  $\frac{1}{4}$  sec
- d)  $\frac{1}{8}$  sec
- e) None of the above

8. Given that

\_\_\_\_\_

and that  $y$  is proportional to  $x^2$  determine the constant of proportionality.

- a)  $\frac{1}{2}$
- b)
- c)  $\frac{1}{4}$
- d)
- e) None of the above



e) None of the above

12. Find all values of  $a$  that satisfy the equation

$$\int_0^a x^2 - 4x \, dx = \int_a^4 x^2 - 4x \, dx.$$

a) -

b) -

c)

d) -

e) None of the above

13. The graph of  $f(x) = \frac{1}{x^2 - 4}$  has

- I. a vertical asymptote at  $x = 2$ .
- II. a horizontal asymptote at  $y = 0$ .
- III. an infinite number of zeros.

a) Only I

b) Only II

c) Only III

d) Only II and III

e) None of the above

14. Find the limit:

\_\_\_\_\_

b)

c)

d)

e) None of the above

15. Find the derivative of the function

e) None of the above

16. Find the definite integral:

—  
\_\_\_\_\_

a) —

b) —

c) —

d) —

e) None of the above

17. Given that find —.

a) —

b) —

c)

d)

e) None of the above

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**Reminder**

Question 20 will be used as a tie-breaker, if necessary.

20. Use properties of the natural logarithm to compute

\_\_\_\_\_

Leave your answers in terms of *natural logarithm* only.

- a)
- b)
- c)
- d)
- e) None of the above

21. Assume





- d) —
- e) None of the above

26. For what values of the numbers  $a$  and  $b$  does the function  $f(x) = ax^2 + bx + c$  have the maximum value

- a)  $a > 0$  and  $b > 0$
- b)  $a < 0$  and  $b > 0$
- c)  $a < 0$  and  $b < 0$
- d)  $a > 0$  and  $b < 0$
- e) None of the above

27. Find the definite integral:

$$\int_0^1 x^2 dx$$

- a)  $\frac{1}{3}$
- b)  $\frac{1}{6}$
- c)  $\frac{1}{2}$
- d)  $\frac{1}{4}$
- e) None of the above

28. The oil in a spherical tank 50 feet in diameter is 20 feet deep. How much oil does the tank contain?

- a)  $\frac{62500}{3}$
- b)  $\frac{31250}{3}$
- c)  $\frac{22000}{3}$
- d)  $\frac{78125}{24}$

e) None of the above

29. Find the definite integral:

\_\_\_\_\_

a)

b)

c)

d) -

e) None of the above

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- d) -
- e) None of the above

35. How many inflection points does the curve given by the equation \_\_\_\_\_ have?

- a) No inflection points
- b) Exactly one inflection point
- c) Exactly two inflection points
- d) Exactly three inflection points
- e) None of the above

36. Suppose \_\_\_\_\_ for any real number. How large can \_\_\_\_\_ possible be?

- a)
- b)
- c)
- d)
- e) None of the above

37. The line tangent to the graph of the function \_\_\_\_\_ at the point with the  $x$ -coordinate \_\_\_\_\_ crosses the  $y$ -axis at the point with the  $y$ -coordinate \_\_\_\_\_.

- a) -
- b) -
- c) -

- d) —
- e) None of the above

38. Given that \_\_\_\_\_, find the definite integral:

- a) —
- b) —
- c) —
- d) —
- e) None of the above

39. Find the area of the region cut off from the parabola \_\_\_\_\_ by the chord joining the points \_\_\_\_\_.

- a) —
- b) —
- c) —

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b)

c)

d)

None of the above